

# **Notional Funding: How an Imaginary Pension Fund Can Help Steer a PAYG System**

**Ismo Risku**

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## ABOUT ME



Ismo Risku

Finnish Centre for  
Pensions

- **Ismo Risku** is a head of planning in Finnish Centre for Pensions, a central organisation of the Finnish earnings-related pension system. He has been working in the Finnish Centre for Pensions since 1999. His responsibilities include long term assessments of the Finnish pension system. He is a Fellow of the Actuarial Society of Finland.

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## ***The basic idea of notional funding***

- Assume a pension system with well-defined benefit rules, including:
  - (a) Information on pensions already accrued
  - (b) Accrual rules for present-day workers
  - (c) Financing based mostly on PAYG (Pay-As-You-Go) principle
- Given points (a) and (b), it becomes possible to determine the pension liability and calculate the actuarial cost of annual accruals
- A contribution level in notional funding (NF) system consists of two components:
  - (a) Full funding contribution, corresponding to the value of the annual accrual
  - (b) An additional contribution to compensate for any missing returns on assets
- The NF system aims to avoid unsustainable growth of net liability (liability minus assets)
- The NF system aims to avoid too high or too low pension contributions
- In essence, pension financing is approached as a debt management challenge

## **General background**

- Consider a defined benefit pension system primarily financed by a pay-as-you-go (PAYG) system supplemented with some assets
- Population ageing challenges PAYG financing
- Low real interest rates challenge funding
- These two elements may cause problems, if corrective measures are not implemented consistently and in a timely manner
  
- Population ageing is the result of:
  - (a) Declining fertility rates
  - (b) Declining mortality rates
  
- I will focus on the effects declining fertility rates:
  - (a) This serves as a simplifying assumption
  - (b) Furthermore, a sensible response to declining mortality rates might involve an increase in the retirement age and a reduction in annual pension accruals

## ***Specific background in Finland (1/2)***

- Over 90% of Finland's pension provision is based on earnings-related mandatory pensions:
  - a) The system is defined benefit
  - b) Financing is primarily through a PAYG (Pay-As-You-Go) system
  - c) Assets approximately equal 8 years of pension expenditure
- Due to the DB principle, contributors bear the risks
- Declining work force is a significant problem
  - a) In 2010 total fertility rate was 1,9 and now it is approximately 1,3
  - b) Immigration alleviates the problem, but hardly solves it
- There is a desire to increase investment risks to boost expected returns
- While this policy seems sensible, it will also increase the risks transferred to younger generations

## ***Specific background in Finland (2/2)***

- In Sweden, contribution rates are fixed while benefits are flexible
- Finnish life expectancy coefficient is adopted from Sweden
  - It adjusts the initial pension levels in accordance with life expectancy
  - In the future, both retirement age and benefit levels will be adjusted in line with life expectancy
- Because of the baby bust, the sustainability of the pension system is facing challenges
- The Finnish government aims to strengthen pension financing through a rule-based adjustment system
  - Specific details are under consideration
- Notional Funding is one rule based system
  - So far NF is just a concept
  - It is possible that it remains just a concept
  - I hope this presentation will clarify the ideas
  - All comments, including critical ones, are welcomed!

# *Notional Funding model*





## ***Benefit rules***

- To illustrate the NF model, we need specific benefit rules:
  - (1) There is only an old-age pension available, starting at the age of 65 years
  - (2) The accrual rate is set at 1.5 % per year
  - (3) Both accrued pensions and pension in payment are indexed to consumer prices
- Real world benefit rules tend to be much more complex
- However, simple benefit rules are useful when seeking to understand how financing rules operate

## The basic idea formally (1/3)

The liability of the system  $L_i$  evolves according to the equation:

$$(1) \quad L_1 = L_0(1 + i) - e_1 + \Delta_1$$

Where

$i$  is the interest rate,

$e_1$  is the pension expenditure on year 1 and

$\Delta_1$  is the capital value of the accrued pensions during the year 1.

The assets of the system  $A_i$  evolve as follows:

$$(2) \quad A_1 = A_0(1 + i) - e_1 + c_1^f + c_1^a$$

Where

$c_1^f$  is the full funding contribution, i.e.  $c_1^f = \Delta_1$

$c_1^a$  is the additional contribution

Now, the problem lies in determining the income from the additional contribution  $c_1^a$

## The basic idea formally (2/3)

The net debt  $L_i - A_i$  evolves according to the equation:

$$L_1 - A_1 = (L_0 - A_0)(1 + i) - c_1^a$$

Let  $g_1^D$  be a targeted growth rate of the net debt from period zero to period one, i.e.,

$$L_1 - A_1 = (L_0 - A_0)(1 + g_1^D)$$

Now we can solve the additional contribution  $c_1^a$ :

$$(3) \quad c_1^a = (L_0 - A_0)(i - g_1^D)$$

A sensible target growth rate  $g_1^D$  should be related to the expected long-run wage bill growth. I will consider the case where  $g_1^D$  equals the expected growth of the present value of the wage bill over a 20-year forward-looking window:

$$g_1^D = \frac{\sum_1^{20} \beta^i \text{wage}_i}{\sum_0^{19} \beta^i \text{wage}_i}$$

Note that the wage bill forecast is based on the observed population

## The basic idea formally (3/3)

To sum up, the evolution of the system is defined by

$$\begin{aligned}
 (1) \quad L_1 &= L_0(1 + i) - e_1 + c_1^f \\
 (2) \quad A_1 &= A_0(1 + i) - e_1 + c_1^f + c_1^a \\
 (3) \quad c_1^a &= (L_0 - A_0)(i - g_1^D)
 \end{aligned}$$

Where

$L_j$  is the liability (year  $j$ )

$A_j$  are the assets

$e_j$  is the pension expenditure on year  $j$  and

$c_j^f$  is the full funding contribution

$c_j^a$  is the additional contribution

$g_j^D$  is the desired growth rate of net liability

$i$  is the interest rate

## ***The legacy cost and the additional contribution***

- PAYG systems lacks assets or have assets that are in sufficient to cover liabilities
- The absence of assets implies a lack of asset income
- This missing asset income is the legacy cost of the PAYG system
- The additional contribution is equal to this legacy cost

## ***Partial funding as a reference model***

- As a reference model, a partial funding (PF) is studied:
  - (1) A specific fraction (30% in our case) of pension benefits are prefunded
  - (2) The rest is financed through a strict PAYG-method
  - (3) If realised return deviates from the assumed return, a retrospective approach is applied
- Everything else, including benefits, population and the economy, remains identical under NF and PF

## ***Population and economy***

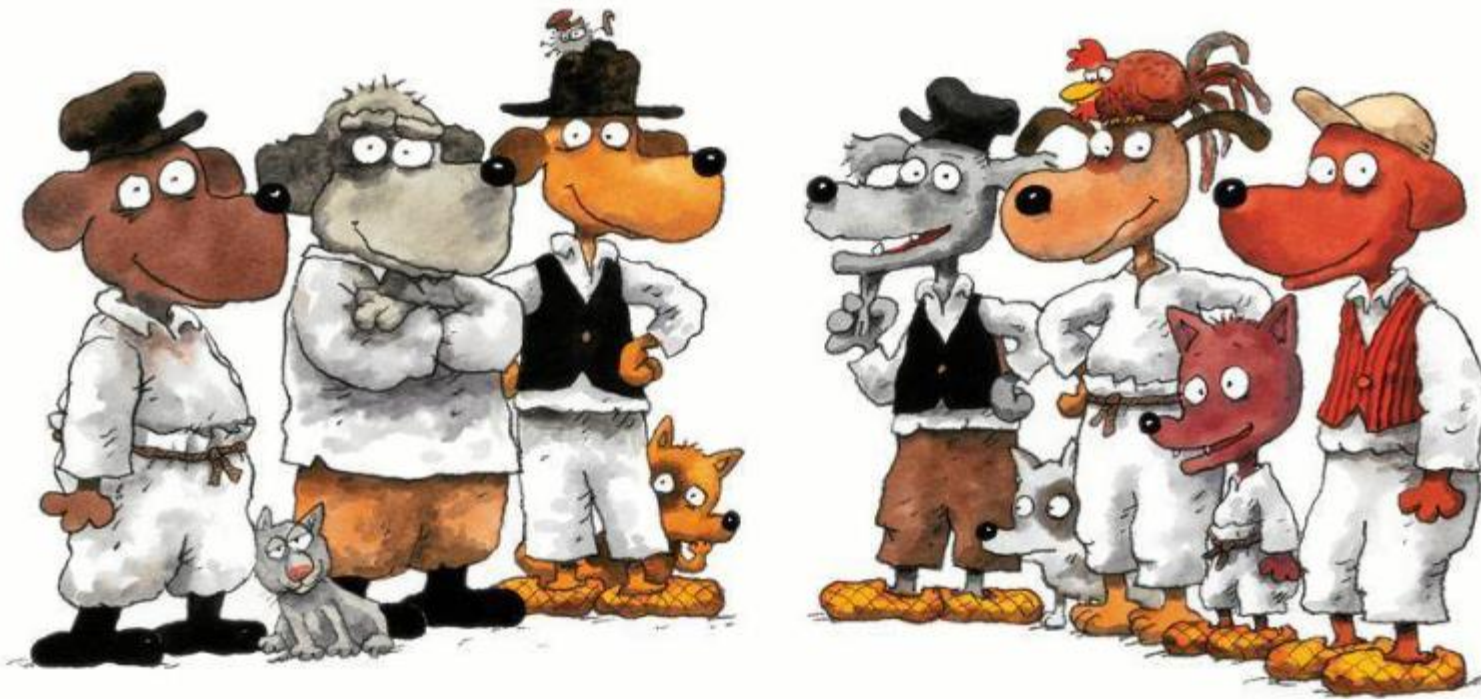
- In order to generate numerical results a population and an economy are required
- Population
  - (1) The mortality rate is zero until the age of 85, after which everyone dies
  - (2) Initially, the population size is equal for each cohort
  - (3) There is no migration
  - (4) We study outcomes under various fertility assumptions
- Economy
  - (1) Working begins at the age of 20 and continues until retirement
  - (2) The wage profile in the next slide
  - (3) The growth rate of real wages is 1.2% per year
  - (4) The contribution rate does not affect wages (in a more realistic setting this should be considered)
  - (5) A risk-free real interest rate of 3% is assumed, but the actual returns on pension assets may deviate from this

## *The wage profile*





# *7 escenarios*



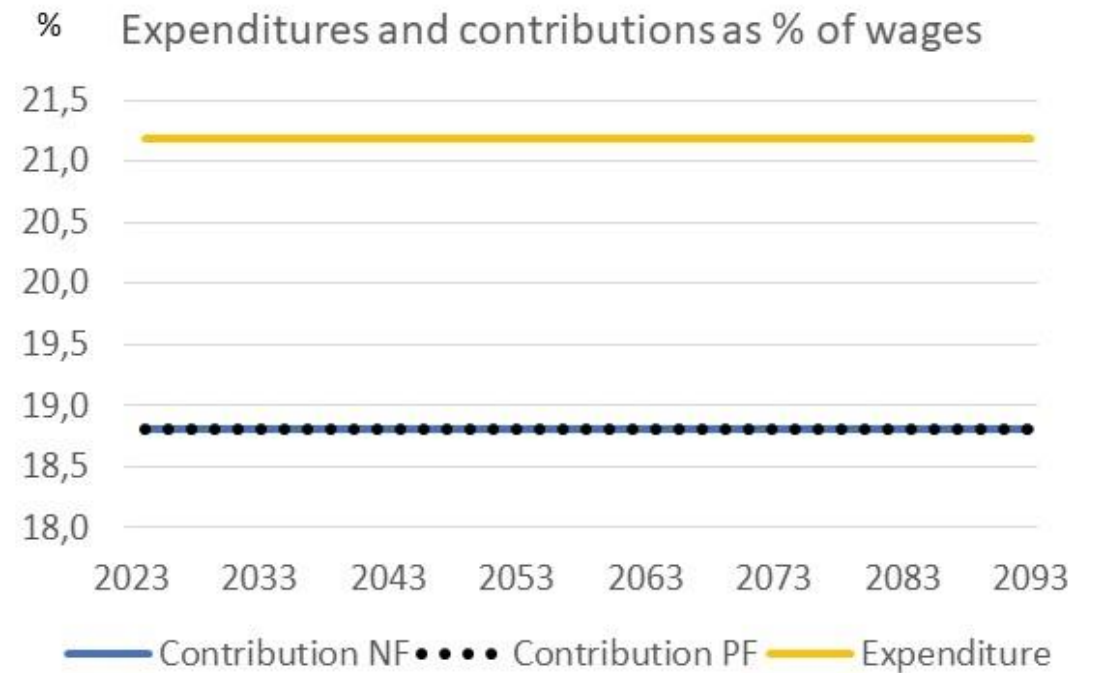
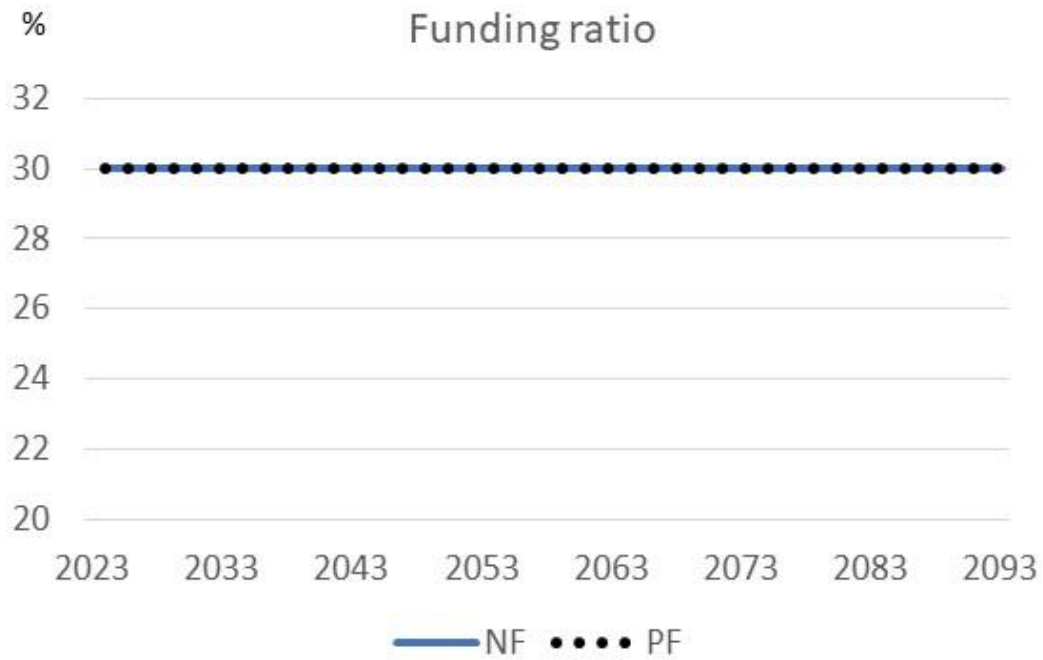
## ***Scenario 1: Constant population, no return deviations***

- This is the simplest illustration
  - (1) The fertility rate is 2 (implying no population growth nor decline)
  - (2) The asset return equals the riskless rate (3 %)
- Essentially, nothing changes as time passes
- NF and PF deliver almost identical outcomes:
  - (1) Expenditures 21.2% relative to wages
  - (2) Contributions 18.8% relative to wages
  - (3) Funding ratio 30 %
- However, there are some differences:
  - (1) The age profile of the contribution rate will be different
  - (2) Intergenerational transfers will be different



## Scenario 1: Constant population, no return deviations

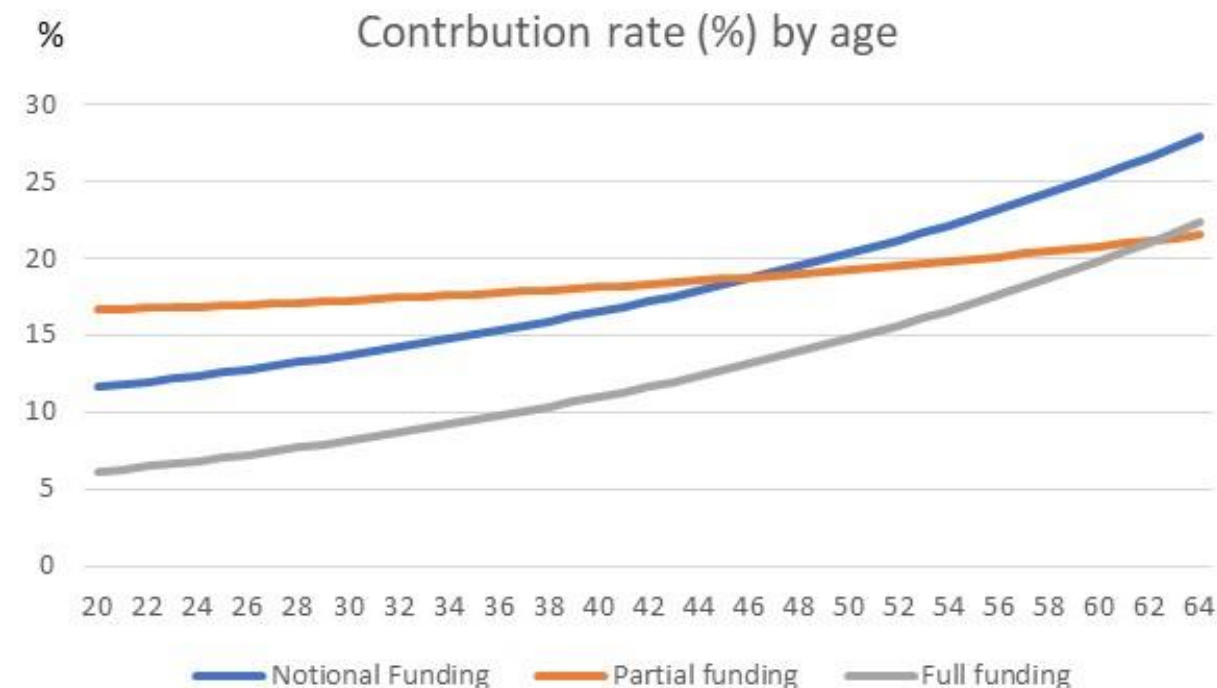
Note: the first simulation year is 2024 in all illustrations



## Scenario 1: Constant population, no return deviations

### Contribution rate by age

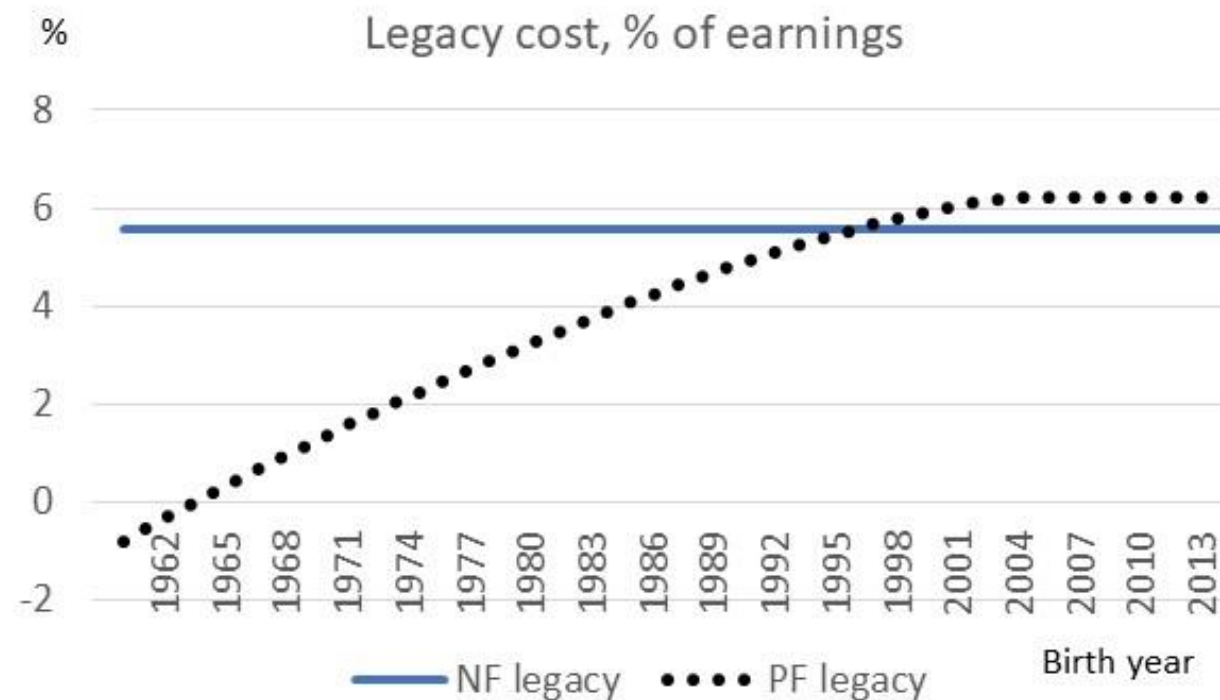
- The contribution rate by age is steeper under NF than under PF
  - In NF, contribution equals full funding contribution plus constant additional contribution
  - In PF, contribution equals 30 % of full funding contribution plus constant PAYG-contribution
  
- The difference between the full funding contribution and actual contribution is the legacy cost
  - Under NF, it isn't age related
  - Under PF, it is highest for the youngest



## Scenario 1: Constant population, no return deviations

### Intergenerational effects

- Benefits are identical under NF and PF
- Therefore we may focus on contributions
- More precisely: the figure displays the present value of the lifetime additional contribution relative to the present value of the lifetime earnings
- This calculation is forward-looking, considering only the future lifetime from 2024 onwards while ignoring the past
- In this scenario, the generational effect arises due to different age profiles of contributions
- In the following scenarios, the average contribution rate in any given year may also differ between NF and PF



## ***Scenarios 2 and 3: transitory return deviations***

Assumptions:

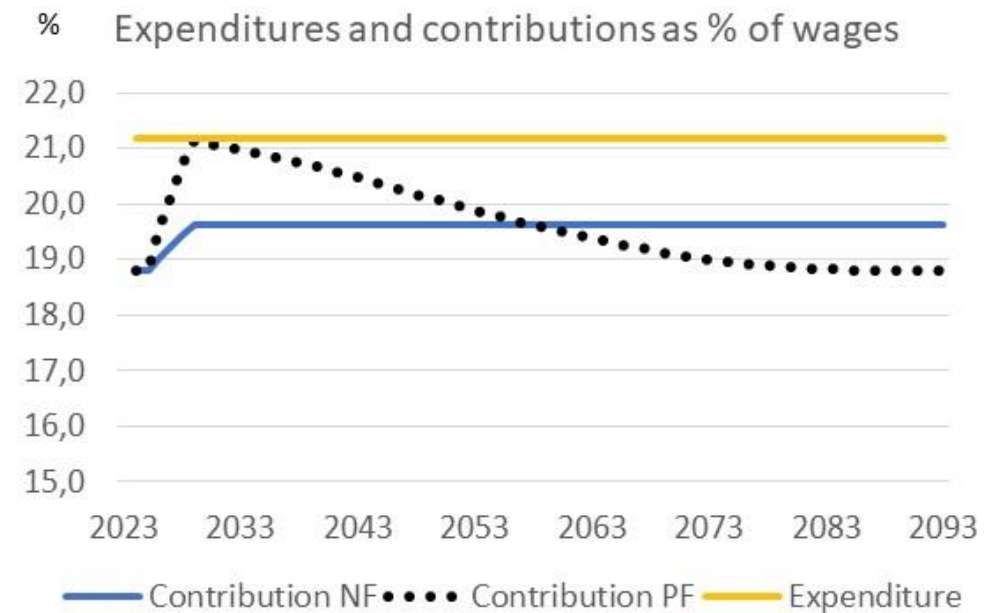
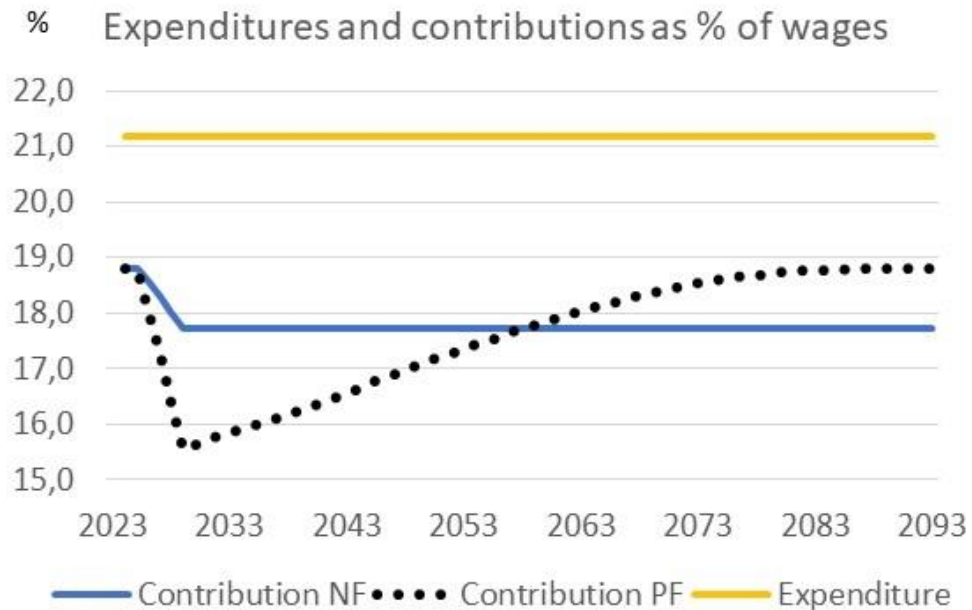
- (1) the fertility rate is 2
- (2) the asset return is + 13 % or - 7 % during 2025-2028  
(i.e. +/- 10 pp. deviation for 4 years)



## Scenarios 2 and 3: transitory return deviations

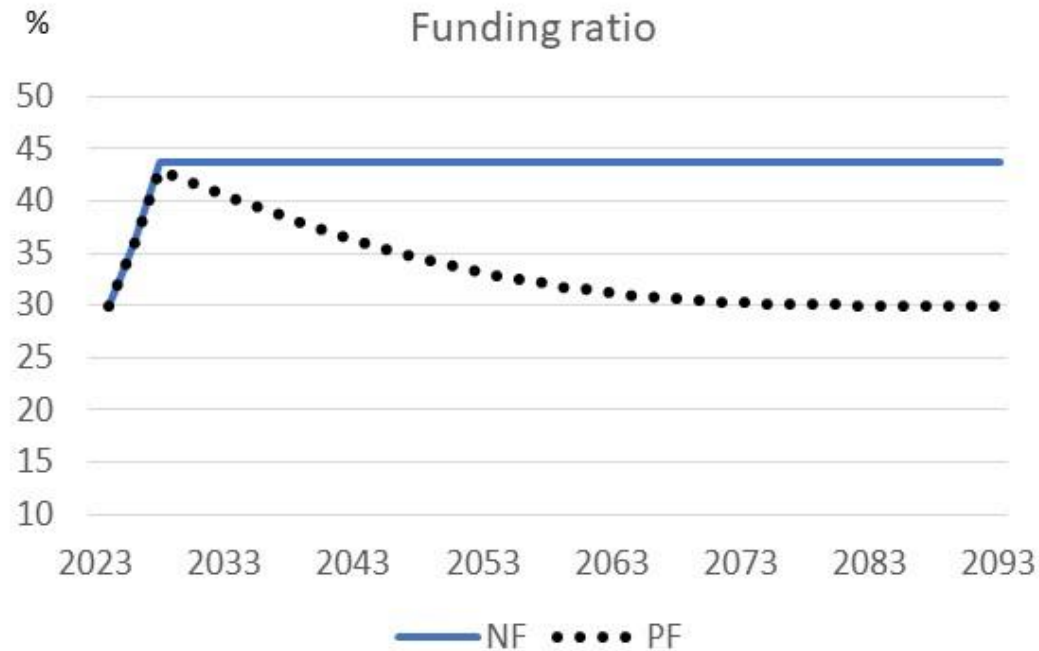
**High return (13 %) yrs. 2025-2028**

**Low return (-7 %) yrs. 2025-2028**

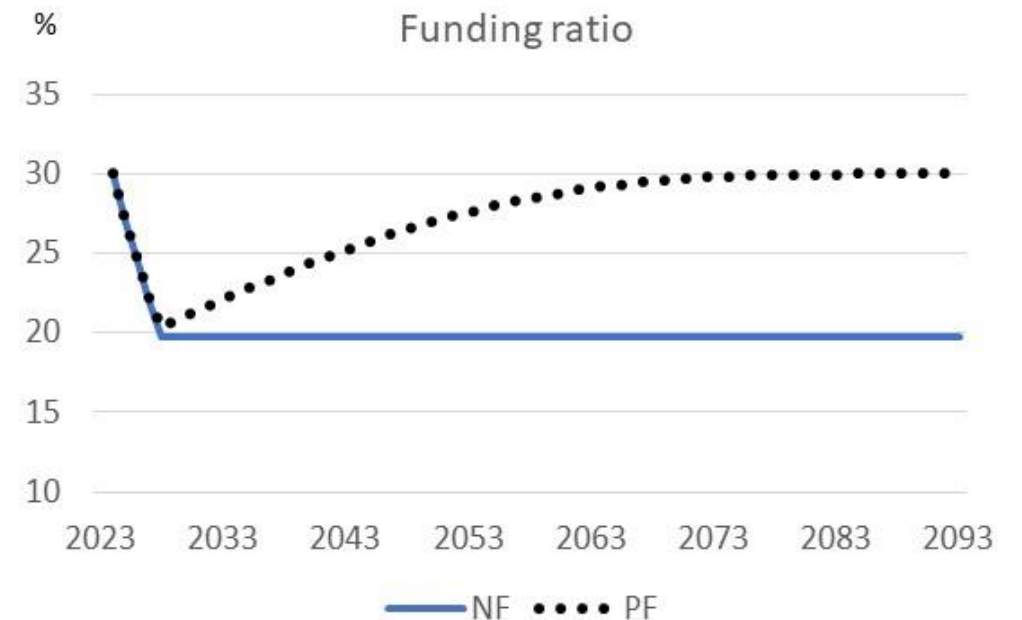


## Scenarios 2 and 3: transitory return deviations

### High return (13 %) yrs. 2025-2028



### Low return (-7 %) yrs. 2025-2028

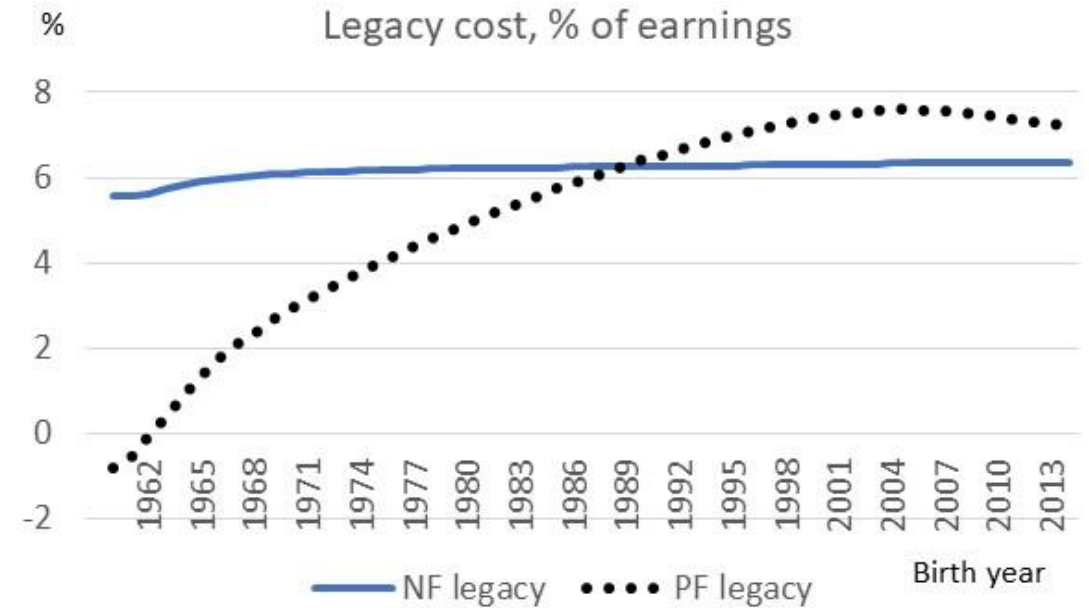
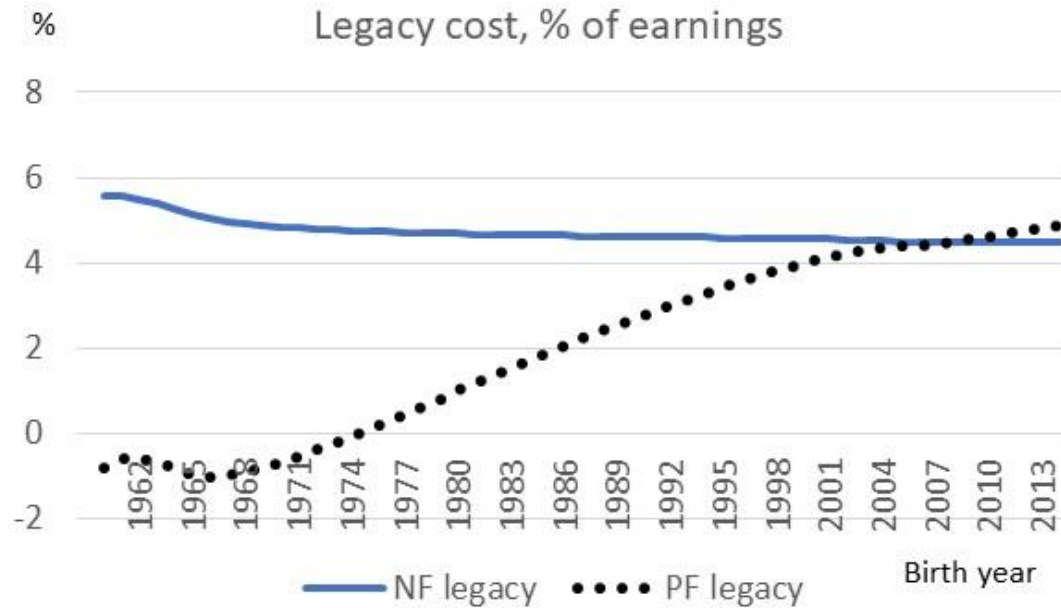




## Scenarios 2 and 3: transitory return deviations

**High return (+ 13 % for 4 years)**

**Low return (-7 % for 4 years)**



## ***Scenarios 4 and 5: low fertility***

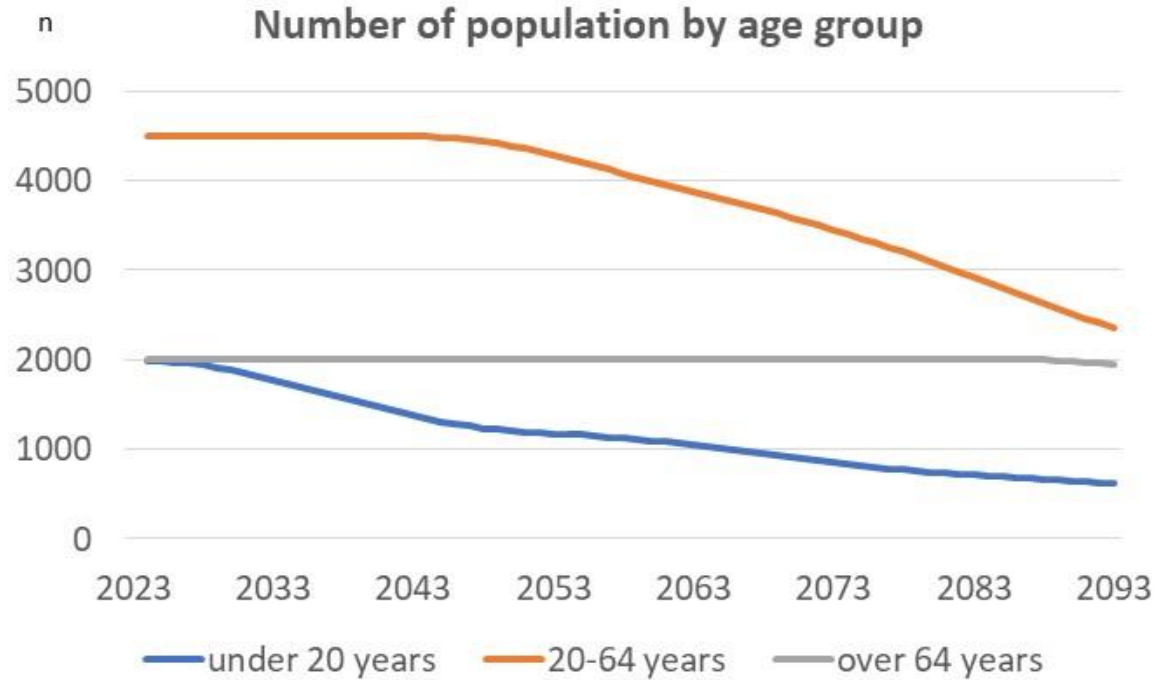
Assumptions:

- (1) the fertility rate drops from 2 in 2023 to 1,2 by 2033 and
  - a) is 1,2 thereafter
  - b) returns to 2 by 2043
- (2) the asset return is 3 %

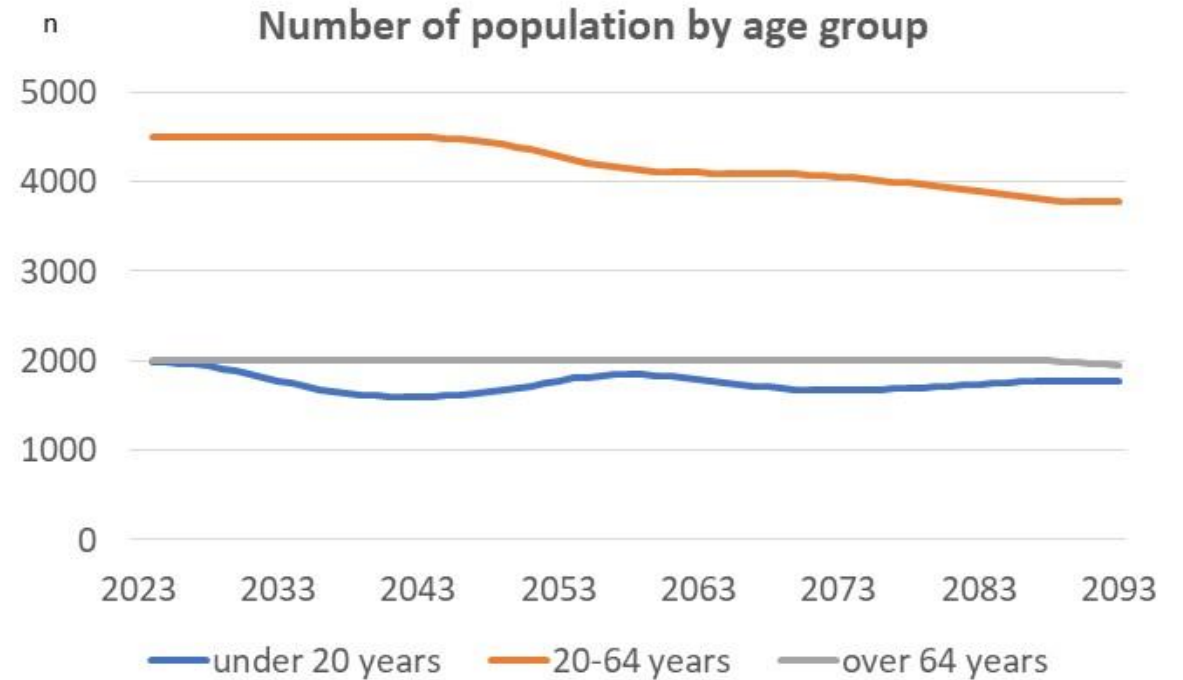


## Scenarios 4 and 5: fertility

### Constant low fertility (TFR 1,2)

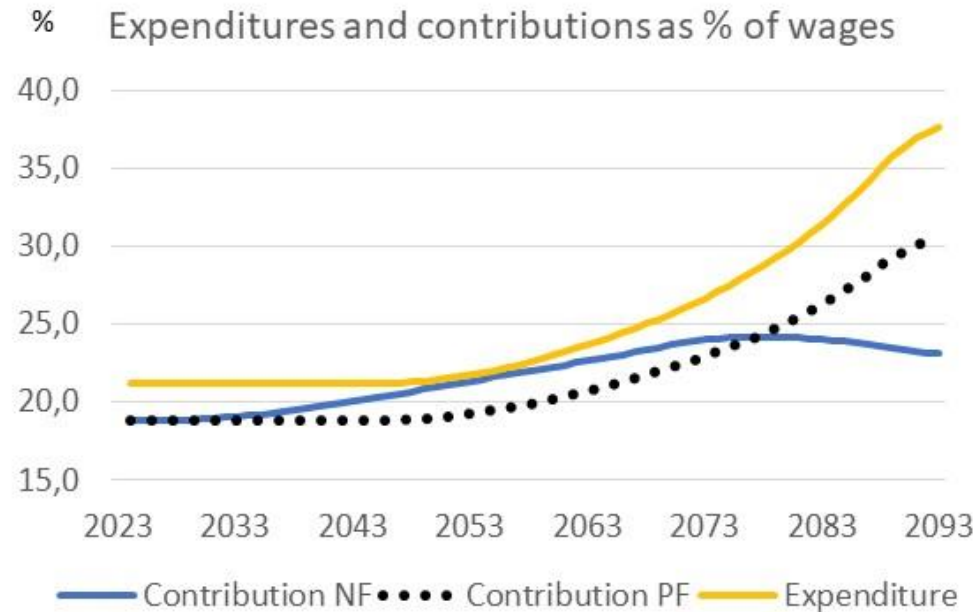


### Transitory fertility shock

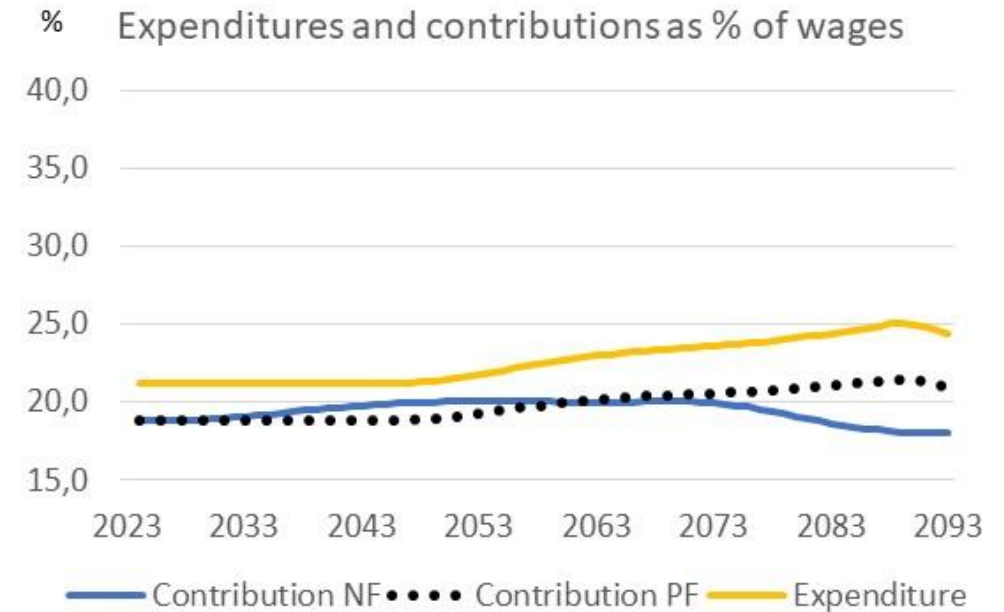


## Scenarios 4 and 5: fertility

### Constant low fertility (TFR 1,2)

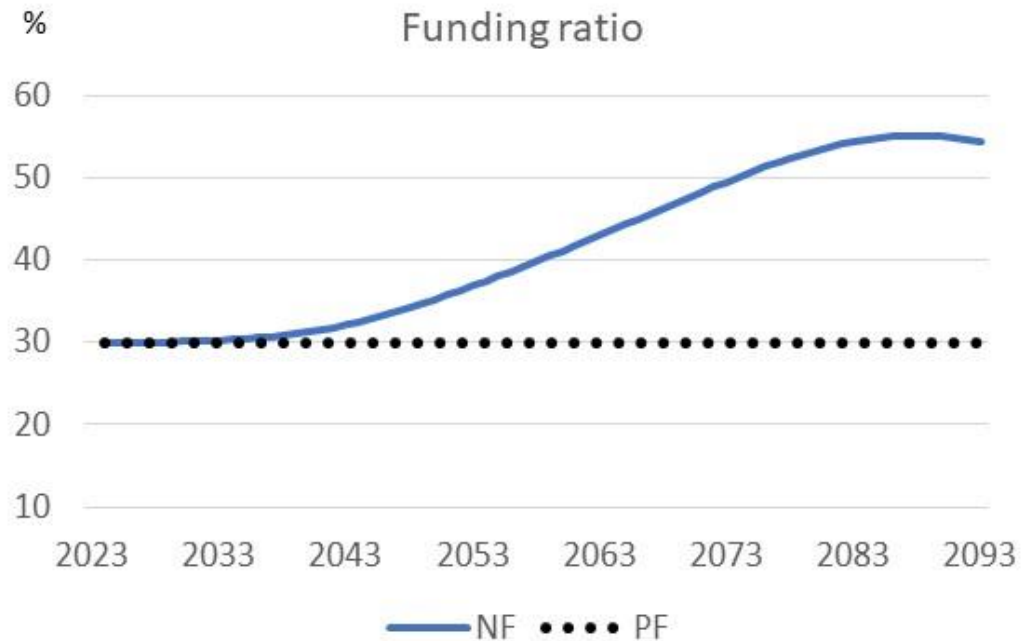


### Transitory fertility shock

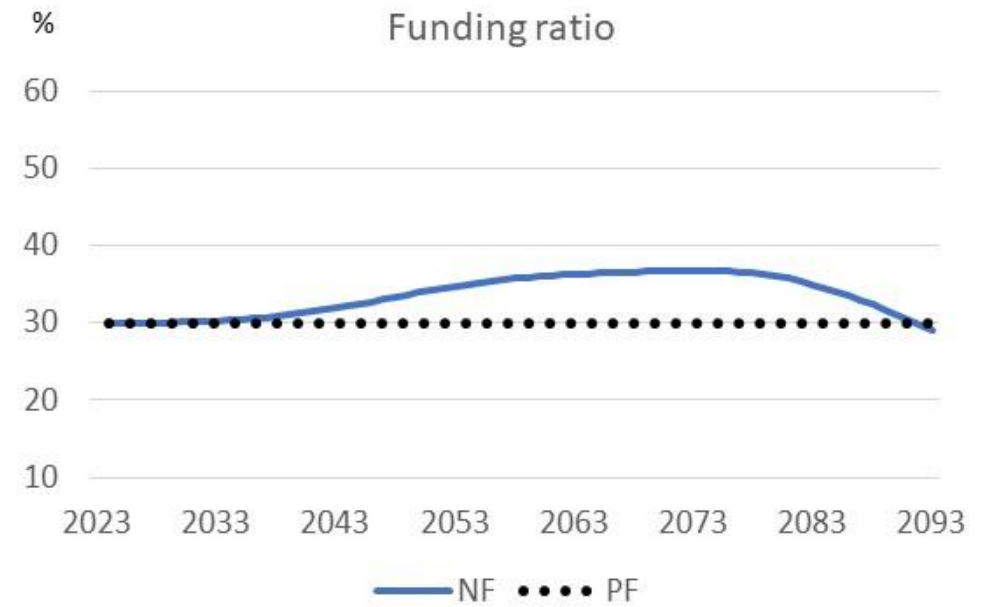


## Scenarios 4 and 5: Funding ratio & fertility

### Constant low fertility (TFR 1,2)

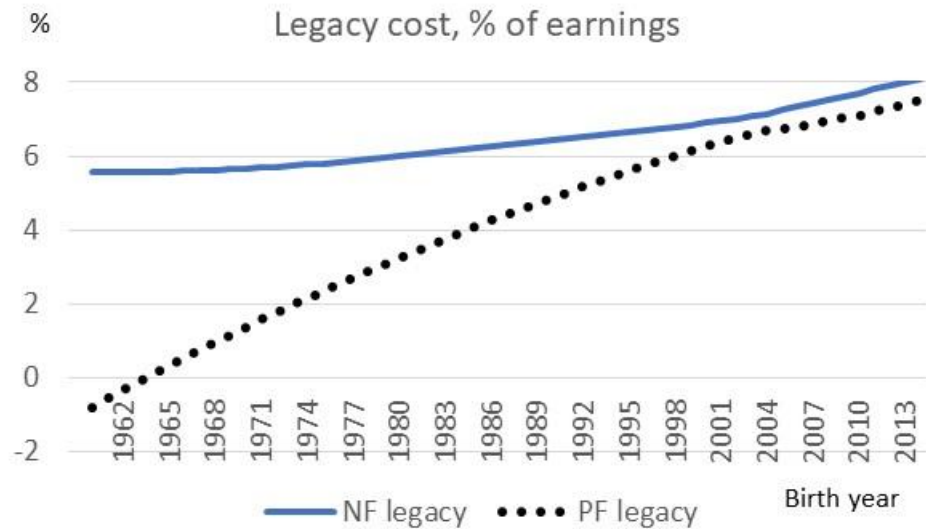


### Transitory fertility shock

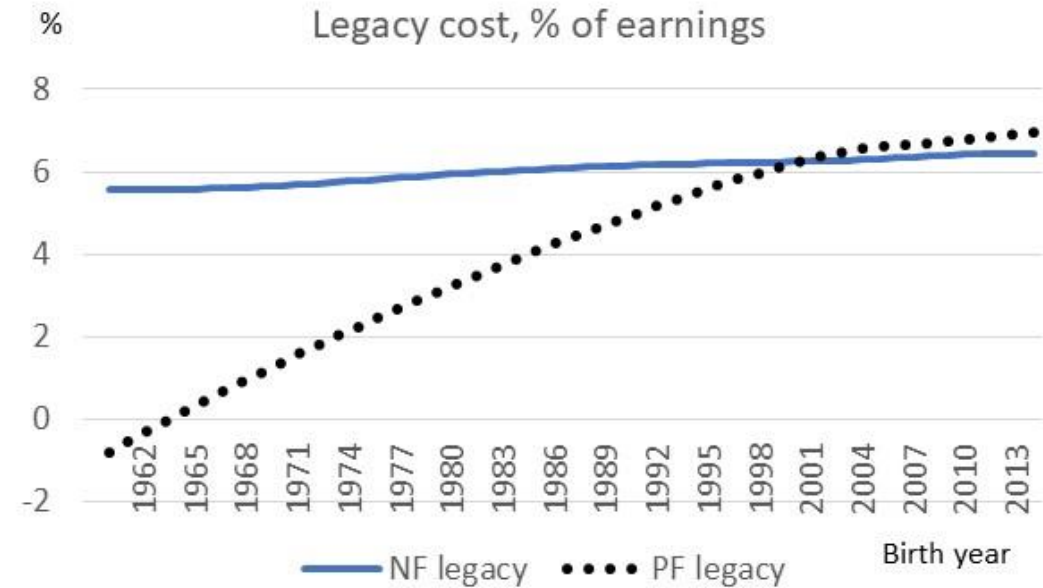


## Scenarios 4 and 5: fertility

### Constant low fertility (TFR 1,2)



### Transitory fertility shock



## ***Scenarios 6 and 7: low fertility with return deviations***

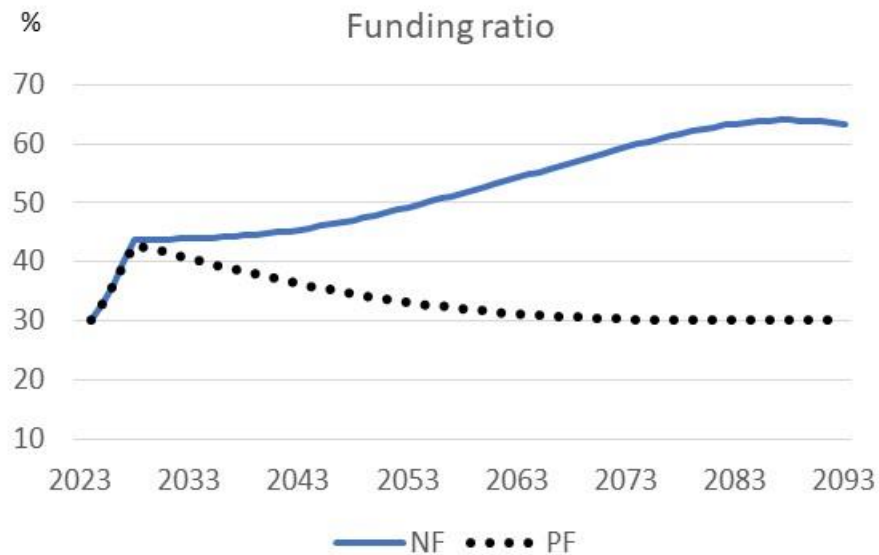
Assumptions:

- (1) the fertility rate drops to 1,2 by 2033 and stays constant
- (2) the asset return is + 13 % / - 7 % during 2025-2028

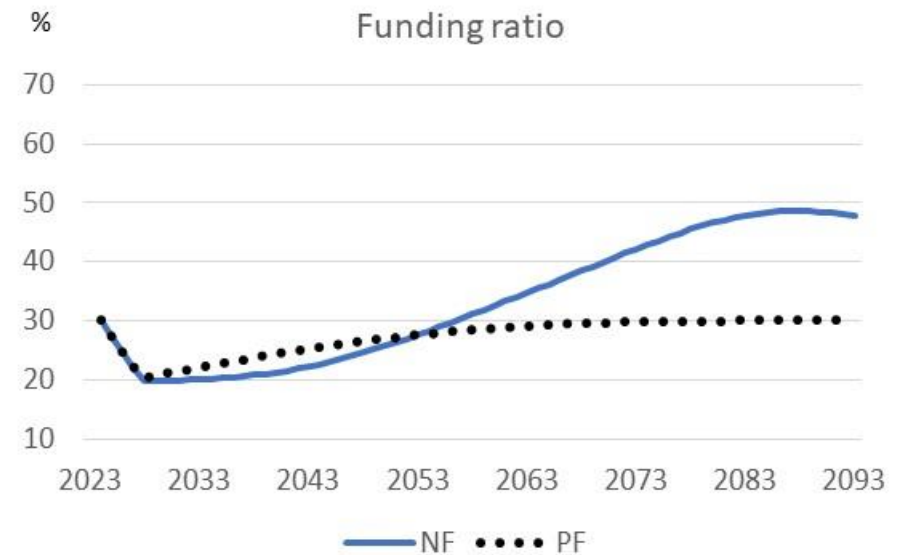


## Scenarios 6 and 7: Funding ratio

### Low fertility and high return



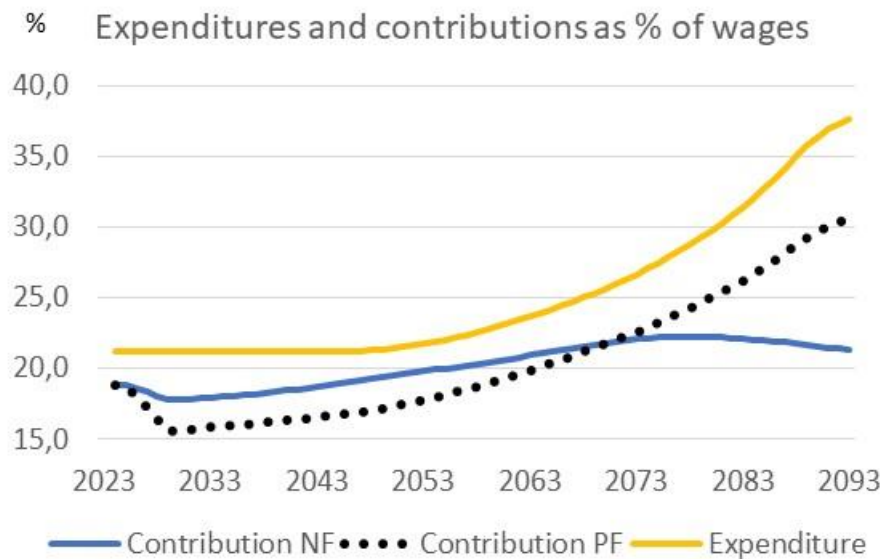
### Low fertility and low return



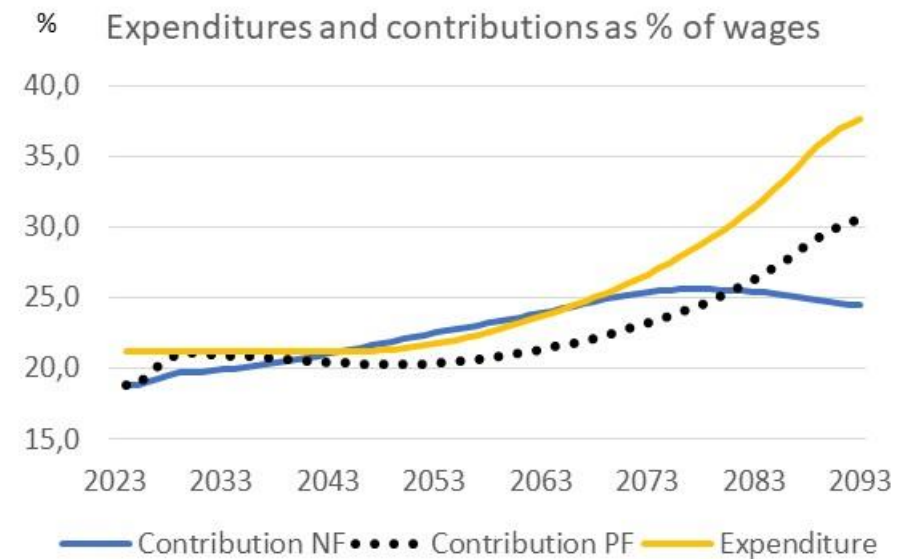


## Scenarios 6 and 7: expenditure and contribution

### Low fertility and high return

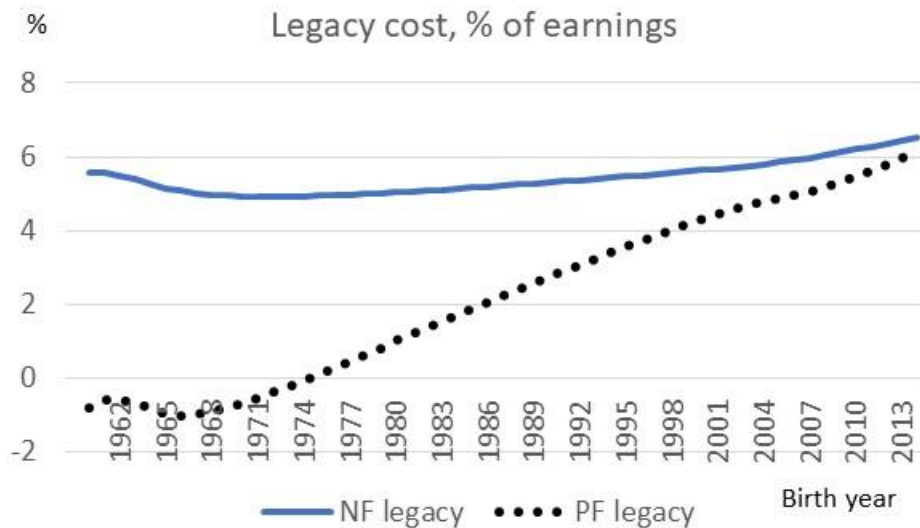


### Low fertility and low return

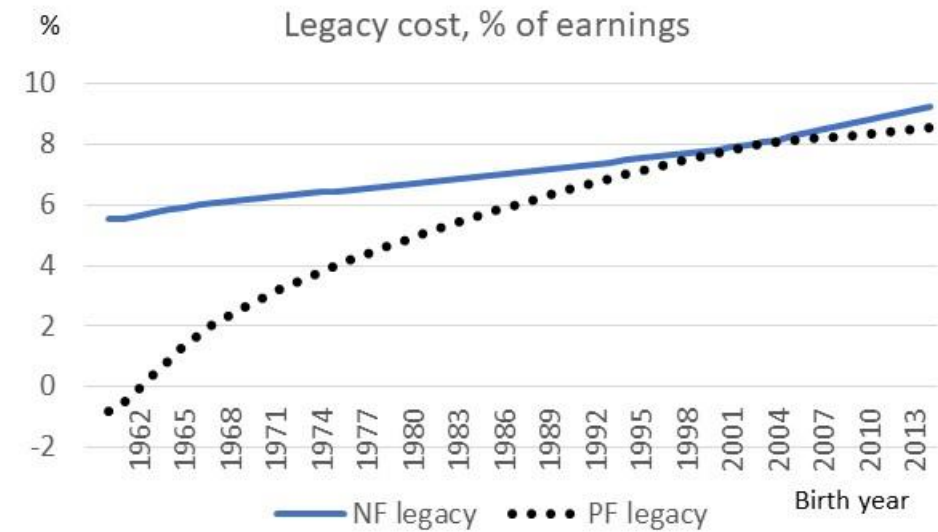


## Scenarios 6 and 7: legacy cost

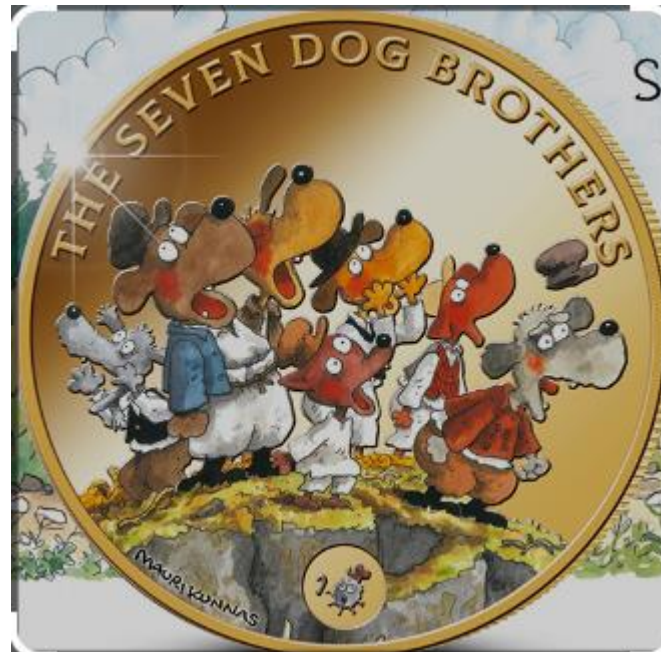
### Low fertility and high return



### Low fertility and low return



# *Benefit adjustment*



## ***Notional funding with benefit adjustment (1/2)***

To reiterate, the evolution of assets and liabilities is defined as follows:

$$(1) \quad L_1 = L_0(1 + i) - e_1 + c_1^f$$

$$(2) \quad A_1 = A_0(1 + i) - e_1 + c_1^f + c_1^a$$

Where  $c_j^a$  is the additional contribution needed to finance the legacy cost

This additional contribution could come from various sources

One particular source is pension benefits

Next, I will study one specific rule for distributing the legacy cost among contributors and beneficiaries

## Notional funding with benefit adjustment (2/2)

I will split the needed additional financing ( $c_1^a$ ) to three components

$$(3) \quad c_1^a = c_1^{ac} + c_1^{af} + s_1^f$$

$c_1^{ac}$  equals 5.55% of wages or less. It will be less than 5.55% if less is enough. In this case other components are zero. This 5.55 % is somewhat arbitrary, but not entirely. In the scenario 1 this is the required additional contribution.

$c_1^{af}$  is a flexible contribution adjuster

$s_1^f$  is a flexible benefit adjuster

These flexible adjusters are interconnected so that pensioners and contributors face similar adjustments in relative terms, i.e.:

$$\frac{s_1^f}{c_1^{af}} = \frac{e_0}{\text{wage bill}_0}$$

This is just one illustration. Other possibly more intuitive solutions might exist.

# ***Scenarios 4, 6 and 7 with benefit adjustment***



## Scenario 4: low fertility

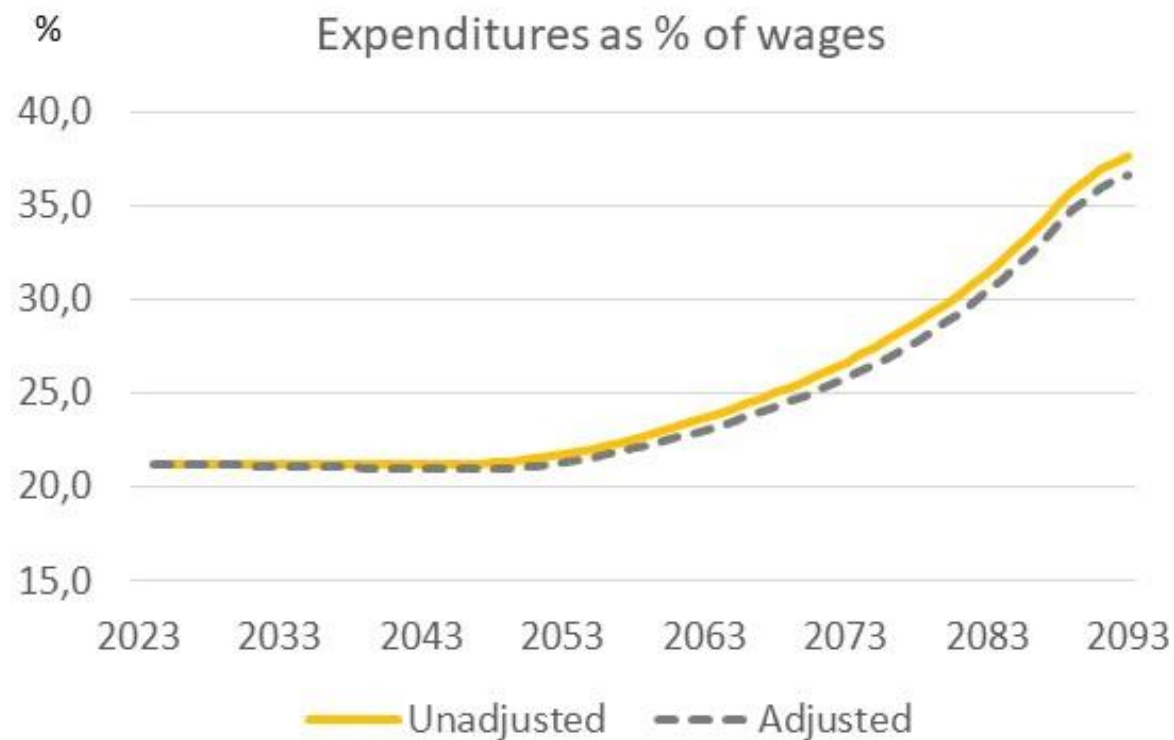
Assumptions:

- (1) the fertility rate drops from 2 in 2023 to 1,2 by 2033 and is 1,2 thereafter
- (2) the asset return is 3 %



### Scenario 4: low fertility

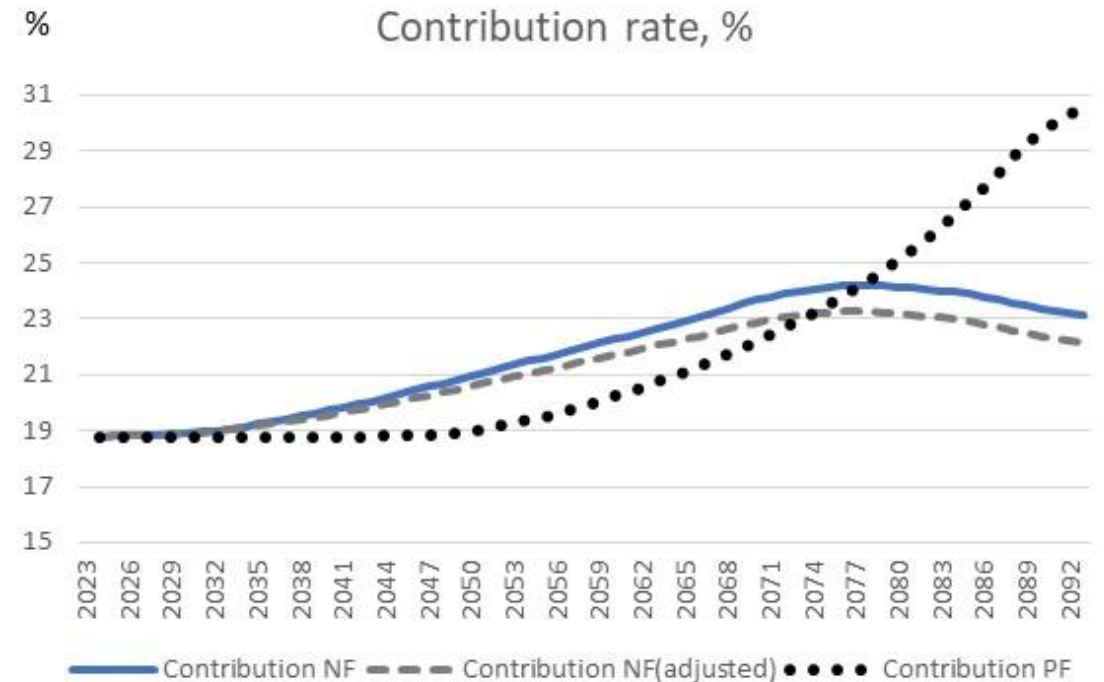
- Benefit adjustment results in modest pension reductions:
- In 2040, the reduction is 1% of benefits
- In 2070s and 2080s, the reduction increases to 3%
- This 3% benefit reduction implies 1%-point reduction in the expenditure ratio





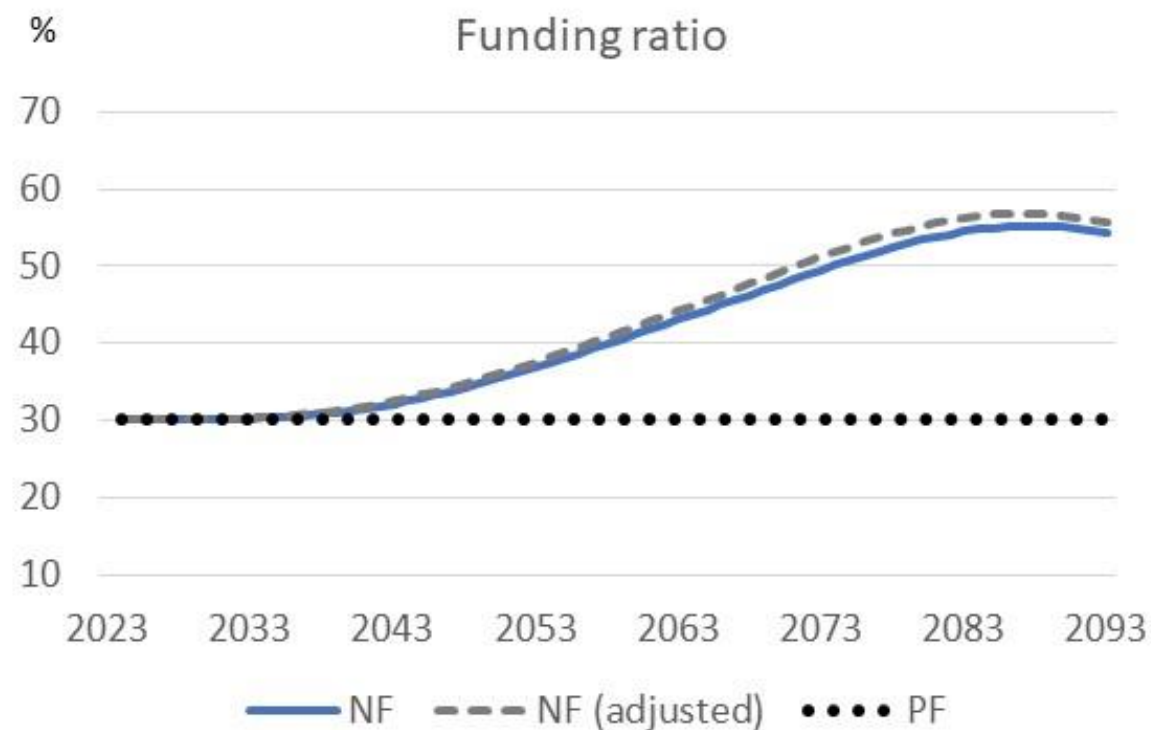
## Scenario 4: low fertility

- Benefit adjustment smooths the contribution rate somewhat (there is an equal reduction in contributions as in expenditures)
- However, the difference between the NF and PF contribution is huge



## Scenario 4: low fertility

- The benefit adjustment results in a slight increase in the funding ratio
- Liability is calculated here, assuming that the existing benefit reduction applies to all accrued pensions as well
- Intergenerational transfers have become more complicated now, as both contributions and benefits are changing
- I will omit the formal intergenerational results
- However, it is evident that the benefit adjustment transfers risks to older generations as well



## Scenarios 6 and 7: low fertility with return deviations

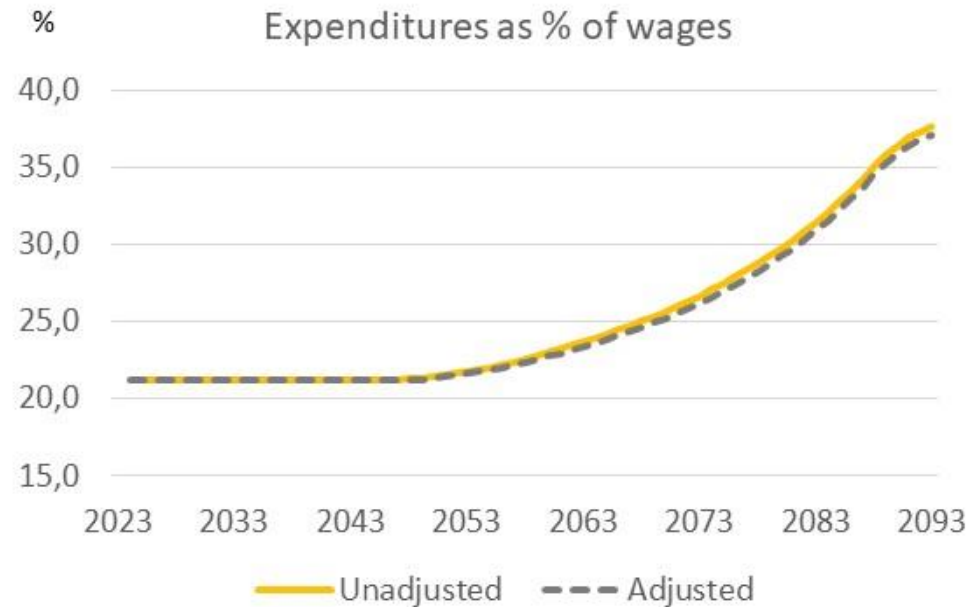
Assumptions:

- (1) the fertility rate drops to 1,2 by 2033 and stays constant
- (2) the asset return is + 13 % or - 7 % during 2025-2028

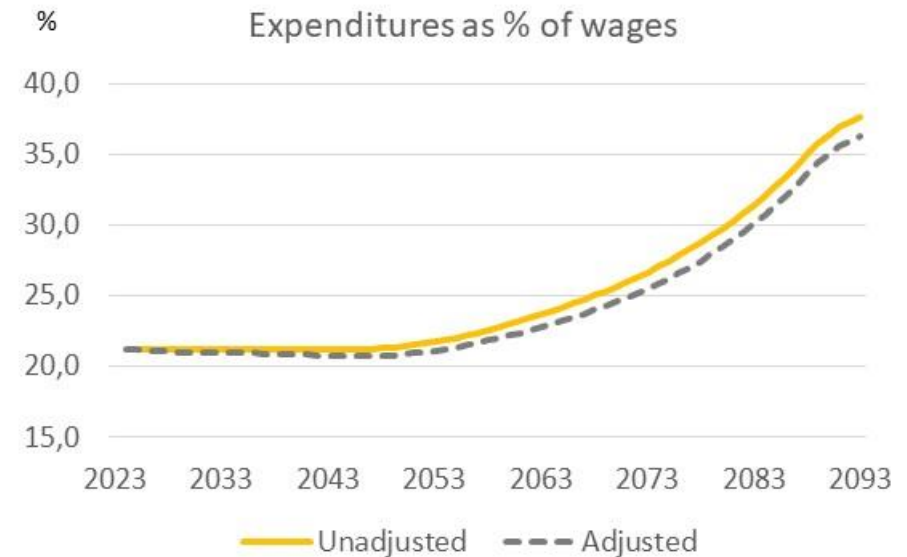


## Scenarios 6 and 7: Expenditures relative to the wage bill

### Low fertility and high return



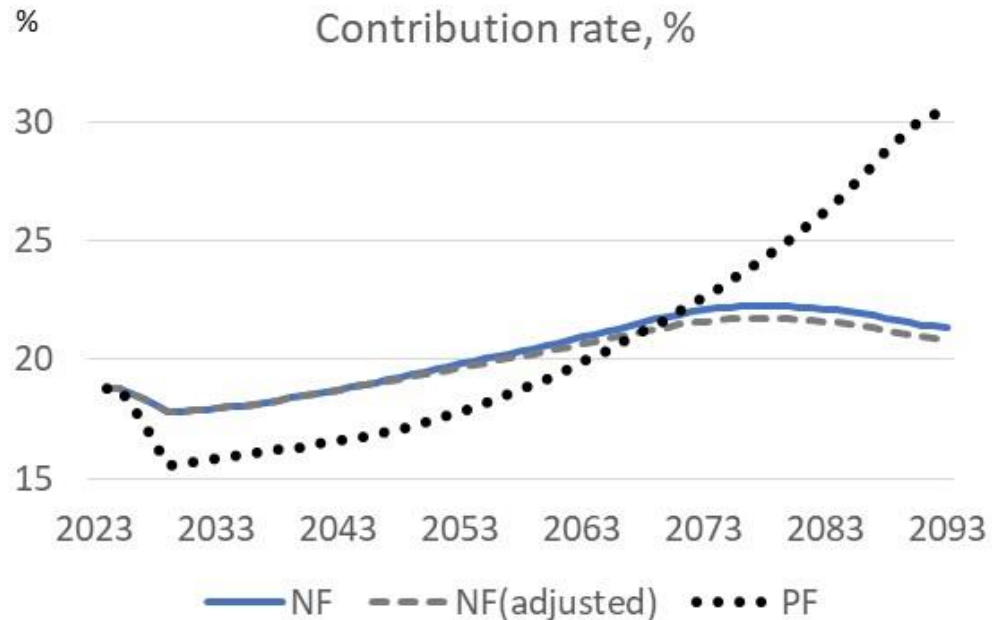
### Low fertility and low return



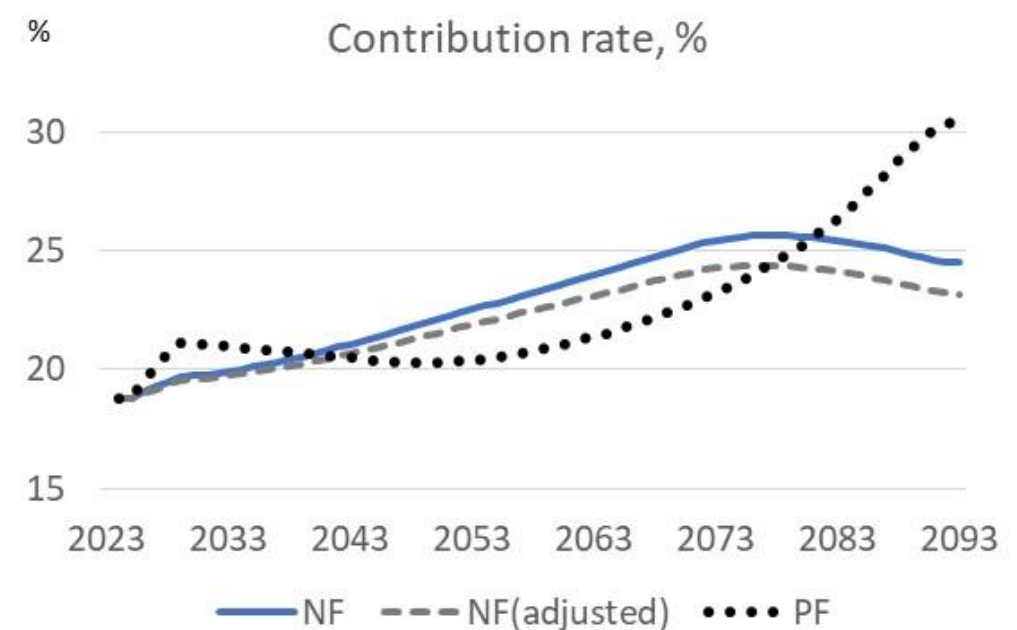
Benefit adjustment depends on returns. In 2080s with low returns 1,3 %-points and with high returns 0,5 %-points

## Scenarios 6 and 7: Contribution rate

### Low fertility and high return

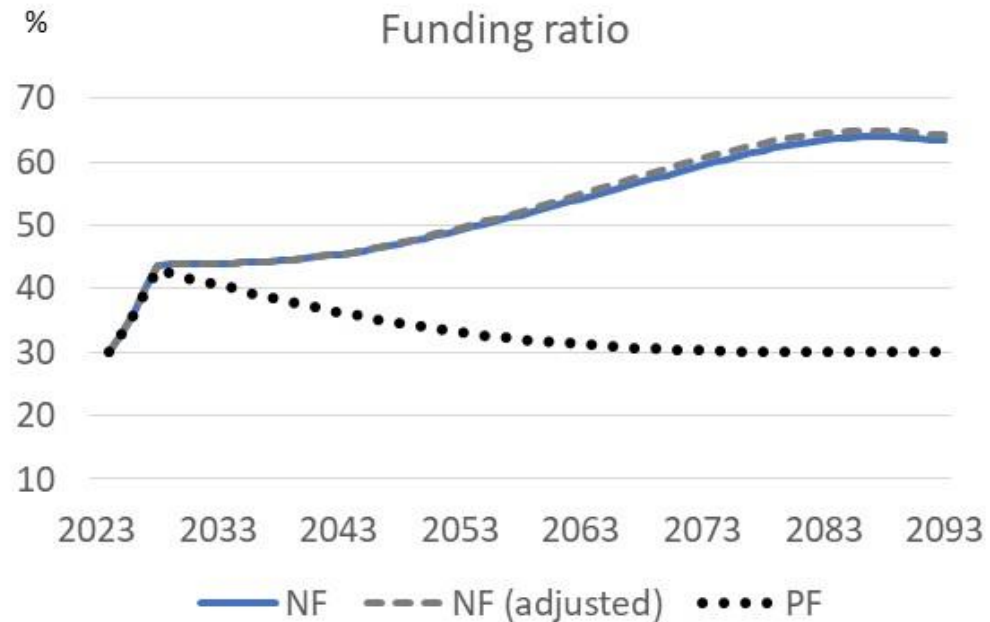


### Low fertility and low return

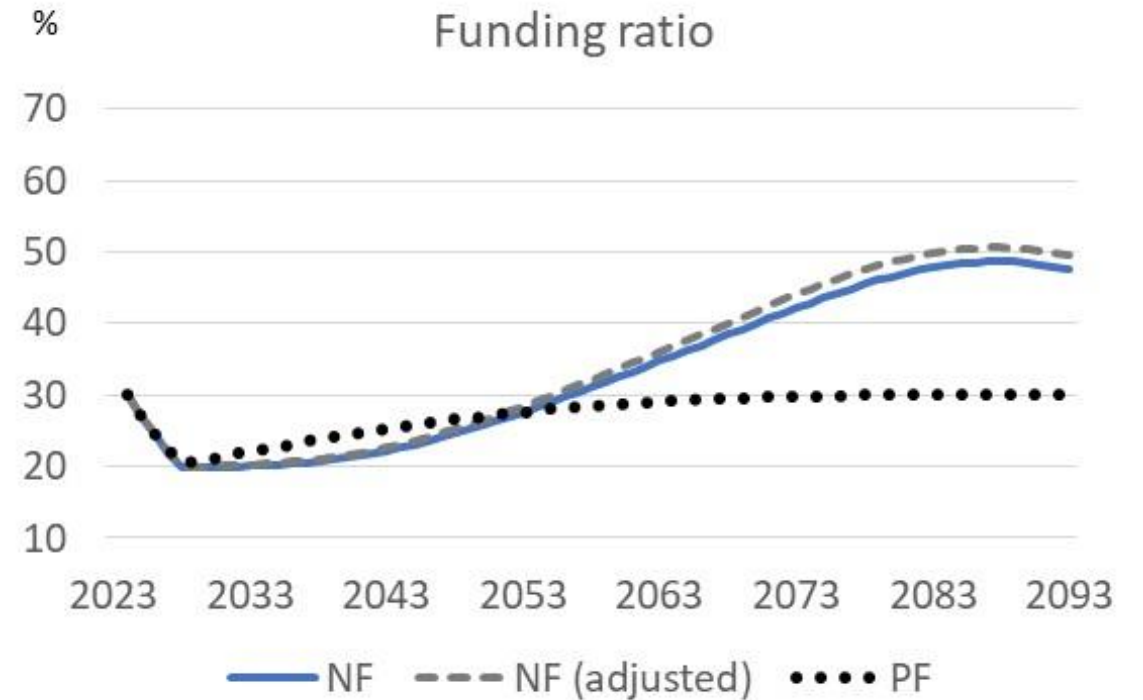


## Scenarios 6 and 7: Funding ratio

### Low fertility and high return



### Low fertility and low return



# *Discussion*



## ***Discussion (1/3)***

- Notional funding applies the logic of funding to a PAYG pension system
- Informational consequences are as follows:
  - (i) The implicit PAYG pension debt becomes explicit
  - (ii) The cost of the implicit debt becomes explicit
  - (iii) All accruals, covered by NF system, must be priced and charged
    - In most social security pension systems, time spent on disability benefits, child care etc., may accrue pension benefits
    - Someone, whether insured collectively or the state, must bear these costs
- This set up implies a rather rigorous and transparent treatment of pension financing
- However, rigorous and transparent system may not be very popular
- Perhaps, in the first place, PAYG pensions are so common because they allow for avoiding such rigor



## ***Discussion (2/3)***

- Discount rate is likely the most important single parameter in NF system
- However, fully funded pensions are more sensitive to changes in the discount rate
- The NF system's foundation lies in PAYG financing, and pure PAYG is not sensitive to fluctuations in the discount rate
  
- If benefits are riskless, then a riskless rate serves as a neutral choice as for the discount rate
- Higher discount rates tend to shift the financial burden toward younger generations
- Often, relatively high discount rates are justified by higher than riskless expected returns
- This rationale, however, ignores the fact that proper valuation of future riskless income streams should be based on riskless rates, regardless of the asset allocation of the pension provider

## ***Discussion (3/3)***

- Intergenerational outcomes were more equitable in each of seven scenarios under NF than under PF (under NF, the legacy cost was relatively stable)
- However, this need not be a universal outcome
  
- The NF approach can be applied to benefit adjustments as well as to contribution adjustments
- In my setup, the role of benefit adjustment was relatively modest
- Nonetheless, benefit adjustment helped to smooth contribution rates
  
- If benefits are adjusted, they are no more riskless
- In this case, it might be logical to apply a somewhat higher discount rate than the riskless rate
  
- I presented NF as an actual tool to set the contribution rate and, potentially, adjust benefits
- One could also use NF as well as a theoretical benchmark for studying an existing pension system

**Thank you!**

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